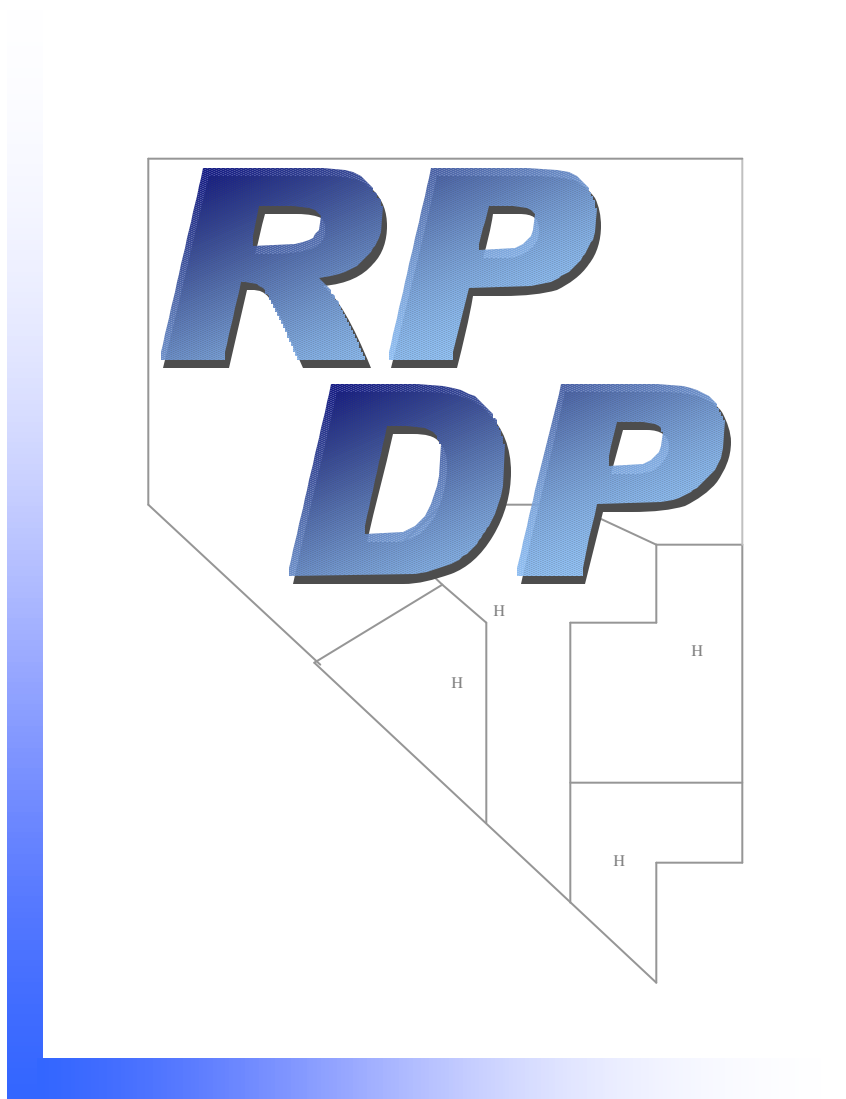


**Southern Nevada
Regional Professional Development Program**

**Serving
Clark, Esmeralda, Lincoln, & Nye County
School Districts**

Strategies for Learning Math Facts



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Learning the arithmetic facts in the first four grades can be pretty hard work. Learning these facts through only rote memorization will make it more difficult than it needs to be. Teaching students strategies to help them memorize the arithmetic facts will make life easier on the kids, their parents, and especially on you.

Before any memorization takes place, the concept for each operation should be explained so the students are comfortable in their understanding.

Addition

Thinking Strategies for Learning the Addition Facts

There are 100 basic arithmetic facts, zero through nine. That's a bunch. But if we use more effective strategies to help students learn, then memorizing these facts will become easier for the students.

- 1. Adding zero:** Students can quickly grasp the rule for adding zero; the sum is always the other number. $8 + 0 = 8$, $0 + 4 = 4$
- 2. Counting on by 1 or 2:** Students can find sums like $5 + 1$ or $6 + 2$ by simply counting on. This thinking strategy allows students to check off 18 of the addition facts. That leaves 63 facts to be learned.
- 3. Combinations to 5:** Students can learn combinations to 5, such as $3 + 2$ or $4 + 1$
- 4. Combinations to 10:** Students can learn combinations to 10, such as $6 + 4$ or $8 + 2$. More facts can be crossed off the list of 100 and we are down to 56 facts to learn.
- 5. Doubles:** For whatever reason, students seem to be able to remember the sums of doubles. That might be a consequence of skip counting in earlier grades. The consequence of knowing doubles is another 6 facts can be checked off our list. That leaves 50 facts to learn, we're halfway home.
- 6. Nines:** It should be pointed out to students that when adding nine, the ones digit in the sum is always one less than the number added to 9. For example $7 + 9 = 16$, the 6 is one less than 7. Another example, $5 + 9 = 14$. 45 facts to go.
- 7. Doubles plus one:** This strategy overlaps the other strategies of doubles and counting on by one. While more sophisticated, students should be taught to use this strategy when the addends are consecutive numbers. For instance, $7 + 8$ becomes $7 + 7 + 1$. Another example, $8 + 9$ becomes $8 + 8 + 1$. That's seven more off the list.

8. **Sharing doubles:** This method works when the addends differ by two. When this occurs it is possible to subtract 1 from one addend and add one to the other addend. This results in a doubles fact that has already been memorized, $7 + 5$ becomes $6 + 6$. Another example, $6 + 8$ becomes $7 + 7$. Some people call the **Sharing Doubles** strategy **Doubles plus two and** attack the problem differently. Using the Doubles plus 2 strategy, $6 + 8$ becomes $6 + 6 + 2$. $7 + 5$ becomes $5 + 5 + 2$. We now have 31 facts left to learn.
9. **Commutativity:** By changing the order, $3 + 4$ to $4 + 3$, it should be pointed out that's an additional 21 facts the students now know. That leaves 10 facts to learn. But it's really five because the commutative property can be used on those 10.

There are other strategies to learning the addition facts. Some teachers might use "Combinations to 5" as a strategy. Rather than using Sharing doubles, some teachers might use "Doubles plus 2". That doesn't matter. What does matter is you make sure students understand the meaning of addition and you develop strategies to help them memorize the facts.

It is expected that students respond automatically when asked a basic addition fact.

Multiplication

Thinking Strategies for Learning the Multiplication Facts

1. **Commutativity:** As with learning the addition facts, order can be changed when learning the multiplication facts. Hence, rather than learning 100 facts, we really only have to learn 55 facts.
2. **Multiplication by zero:** Students can easily grasp that 0 times any number is zero.
3. **Multiplication by one:** Again, the generalization is easy for students to see that 1 times any number is the number.
4. **Multiplication by two:** Students should be taught that multiplying by two is the Doubling strategy used in addition. Using the first four strategies, we have learned 27 more facts; only 28 remain to be learned.
5. **Multiplication by five:** Students can often be taught the fives by referring to the minute hand on a clock.
6. **Squaring:** As with the addition facts, students seem to learn square numbers faster than other facts.
7. **Multiplication by nine:** Patterns emerge when multiplying by 9. One pattern is the sum of the digits in the product is always equal to 9. The other pattern is the ten's

digit is always one less than the factor multiplied by 9. $9 \times 6 = 54$. Notice $5 + 4 = 9$ and the 5 in the product is one less 6, the number being multiplied by 9. Another example, $8 \times 9 = 72$, the sum is 9 and the tens digit is one less than the tens digit. Only 10 facts to go.

8. **Distributive property:** Students should feel comfortable breaking numbers apart and using previously learned information. For instance, 7×6 might be rewritten as $7(5 + 1)$. This would allow a student to use the 7×5 fact that he knows and add that to the 7×1 fact to get 42.
9. **Finger math:** Facing your palms of your hands to your face, let the baby finger become the 6 finger, the ring finger the 7, the middle finger the 8, the index finger be the nine finger. To multiply the 7×7 , place the two ring fingers together. The number of fingers touching and below represent the tens digit. There are four fingers, multiply the fingers above those on each hand to determine the ones digit. That would be 3×3 . The product is 49. Try 7×9 by touching the index finger on one hand with the index finger on the other hand. There are 6 fingers touching or below so the answer is sixty something and you now multiply the fingers on top to get the ones digit. That's 1×3 , the final answer is 63.

There are other strategies for learning the multiplication facts. There are two things I want to point out to you before we go any further. First, you don't have students memorize the multiplication facts until you have taught the concept. Make sure the kids feel comfortable in what they are learning. Second, notice we have not taught the facts sequentially. We taught them in an order to help students learn so students experience a sense of accomplishment.

Subtraction

1. **Fact families:** This strategy works when students understand the relationship between addition and subtraction. When students see $6 - 2$ and think $2 + ? = 6$.
2. **Counting backwards:** This method is similar to Counting on used in addition. It isn't quite as easy. Some might think if you can count forward, then you can automatically count backward. This is not true –try saying the alphabet backwards. Students should only be allowed to count back three.
3. **Zeros:** The pattern for subtracting zero is readily recognizable. $5 - 0 = 5$
4. **Sames:** This method is used when a number is subtracted from itself; this is another generalization that students can quickly identify. $7 - 7 = 0$.

Division

- 1. Fact families:** This strategy works when students understand the relationship between multiplication and division. When students see $24 \div 6$, they have to relate that to $6 \times ? = 24$.

Using the fact strategies presented, students learn the easier facts first that provides successful experiences that build confidence and motivate students to learn more. It's important that students not only understand each operation, but they get off their fingers as quickly as possible. Memorizing the basic arithmetic facts simplifies the process of recalling and allows that information to become automatic. Understanding and critical thought can then be built on this base of knowledge.

The more sophisticated mental operations in mathematics of analysis, synthesis, and evaluation are impossible without rapid and accurate recall of specific knowledge.